QSPR Models of Physicochemical Properties of Natural Amino Acids by Using Topological Indices and MLR Method

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Summary: The mathematical has provided very useful tools for relationships between the structures and molecular properties. Topological indices are numerical parameters of a graph which characterize its topology and are usually graph invariant. In this study the relationship between the Randic' (^{1}X), Balaban (J), Szeged (Sz), Harary (H), Wiener (W), Hyper-Wiener (WW) and Wiener Polarity (Wp)to the thermal energy (E_{th} kJ/mol), heat capacity (C_{V} J/mol K) and entropy (SJ/mol K) of 19 natural amino acids is represented.

Physicochemical properties are taken from the quantum mechanics methodology with HF level using the ab initio 6-31G basis sets. The multiple linear regressions (MLR) and Back ward methods (with significant at the 0.05 level) were employed to give the QSPR models.

After MLR analysis, we studied the validation of linearity between the molecular descriptors in the best models for used properties. The predictive powers of the models were discussed by using the method of cross-validation.

The results have shown that one descriptor (W) could be efficiently used for estimating the entropy (S), heat capacity (Cv) and Wiener Polarity index could be used for modeling and predicting the thermal energy of respect compounds.

Keywords: Topological indices; Natural amino acids; Multiple linear regression; QSPR; Validation.

Introduction

Amino acids (AAs) the building blocks of proteins, molecules that contain amine and carboxyl functional groups play an important role in biology such as: synthesis of proteins [1, 2], intermediates of metabolic pathways [3], neurotransmitters [4, 5], antibiotics [6, 7]. The standard amino acids were mostly investigated.

Quantitative Structure- Property Relationship (QSPR) and Quantitative Structure-Activity Relationship (QSAR) methods are based on the hypothesis that change in chemical structure of a compound is reflected in change to its physico-chemical properties [8].

Topological indices (TIs) proposed by the group of mathematical chemists that is final result of a logic and mathematical procedure which can be used for translating chemical constitution into numerical values for QSPR /QSAR studies. Topological descriptors to be calculated for any set of molecules and must be derived from well-established procedures, which enable molecular. For the use of the topological descriptors, knowledge of chemo-informatics, chemometrics, statistics and the principles of the QSPR approaches is necessary.

Revived interest in Tls is apparent from numerous recent reviews [9-12, 13].

Peptides and analogues QSAR modeling has been used to estimate antimicrobials and angiotensin -converting enzyme (ACE) inhibitors [14].

The oxytocin vasopressin analogues of 20 natural amino acids have been investigated by using semi-quantitative descriptors [15].

Two-dimensional descriptor for QSAR studies of amino acids includes ten orthogonal factors (TOF) has been developed [16].

QSAR studies for prediction hydrophobic, steric, and electronic properties of 20 coded amino acids by using a new set of descriptors and multiple regression method combined with partial Least Squares regression (PLS) have been reported [17].

Amino acids descriptors such as Divided Physico-chemical Property Scores (DPPS), Vectors of Hydrophobic, Steric and Electronic properties (VHSE) were applied to QSAR study of 214 tripeptides. PLS method is applied for prediction of antioxidant activity of tripeptides [18].

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A new topological scale (T-scale) for the studies on structure-activity of 135 amino acids has been examined [19].

New topological descriptors were calculated for predicting the relationship between structure and biological activity of 87 amino acids [20].

A new molecular descriptors based on quantum topological molecular similarity (QTMS) parameters of amino acid has been applied for modeling of peptides and best models were established [21].

The main aim of this work is to illustrate the usefulness of topological descriptors in QSPR study of natural amino acids. As far as we are aware, this is the first QSPR study for prediction physicochemical properties such as the heat capacity (Cv), thermal energy and entropy of natural amino acids using topological indices.

Experimental

Quantum Chemical Computations

The chemical structure of the AAs was drawn by Gauss View Software and then was transferred into Gaussian03 program to optimize the physicochemical properties of the molecules at the RHF/6-31 G level of theory.

The heat capacity (Cv), entropy (S) and thermal energy (E_{th}) of nineteen essential (AAs) is taken from the quantum mechanics methodology are listed in Table-1.

Table-1: Amino acids and their heat capacity, entropy

and thermal energy used in present study.

Comp.	C	S	C _v	E _{th}
No	Compounds	(J/mol.K)	(J/mol.K)	(kJ/mol)
1	Alanine	335.929	97.657	320.347
2	Arginine	504.868	198.993	617.992
3	Asparagine	389.901	136.38	408.779
4	Aspartic acid	383.088	127.92	382.800
5	Cysteine	370.331	117.332	323.607
6	Glutamine	433.294	151.179	494.042
7	Glutamic acid	473.731	168.88	457.129
8	Glycine	309.169	76.356	237.779
9	Histidine	429.624	148.54	480.917
10	Isoleucine	415.053	155.851	570.842
11	Leucine	403.027	141.447	567.268
12	Lysine	456.556	173.871	623.819
13	Methionine	441.638	157.783	495.184
14	Phenylalanine	439.163	163.759	564.124
15	Serine	351.032	108.282	338.889
16	Threonine	388.372	135.515	418.309
17	Tryptophane	469.355	195.908	653.915
18	Tyrosine	458.989	181.909	578.499
19	Valine	389.576	137.643	486.677

Topological Indices

Nowadays, in the literature, hundreds of topological indices, suitable to describe different properties, are reported. The topological indices (TIs) used for the QSPR analysis were Wiener (W) [22], Szeged (Sz)[23], first order molecular connectivity(1X) [24], Balaban(J) [25], Hyper-Wiener(WW) [26], Wiener Polarity(Wp)[27] and Harary(H) [28] indices. Moreover, many investigations were carried out with such descriptors [29, 31].

All the used topological indices were calculated using all hydrogen suppressed graph by deleting all the carbon hydrogen as well as hydrogen bonded heteroatoms from the structure of the amino acids. The descriptors were calculated with chemicalize program [32]. Seven topological indices tested in the present study are recorded in Table-2.

Statistical Analysis

Structure- Property models (MLR models) are generated using the multi linear regression procedure of SPSS version 16.0 and backward stepwise regression was used to construct the QSPR models. For drawing the graphs of our results, we used the Microsoft Office Excel – 2010 program.

Regression Analyses

The heat capacity (Cv J/mol K), entropy (S J/mol K) and thermal energy (E_{th} kJ/mol) are used as the dependent variable and ^{1}X , J, H, W, Wp, WW and Sz indices as the independent variables. Criteria for selection of the best multiple linear regression model were the statistics: correlation coefficient (R), squared multiple correlation coefficient (R^{2}), adjusted correlation coefficient (R^{2}), Fisher ratio (F), root mean square error (RMSE), Durbin-Watson value (DW) and significant (Sig).

Results and Discussion

Several linear QSPR models involving three-seven descriptors are established and strongest multivariable correlations are identified by the Back ward step wise regression routine implemented in SPSS 20.0 was used to develop the linear model for the prediction of the physico chemical properties.

Comp.No.	^{1}X	J	H	W	WW	Wp	Sz
1	2.64	2.99	9.33	29	47	4	29
2	5.54	3.2	26.92	247	739	11	247
3	4.04	3.38	17.97	96	206	8	96
4	4.57	3.38	17.97	96	206	8	96
5	3.18	3.14	12	46	83	6	46
6	5.07	3.3	20.87	136	330	9	136
7	5.07	3.3	20.87	136	330	9	136
8	2.27	2.54	6.67	18	28	2	18
9	5.2	1.98	25.6	165	397	10	182
10	4.09	3.58	18.23	92	188	10	92
11	4.04	3.38	17.97	96	206	8	96
12	4.63	3.13	20.45	143	368	9	143
13	4.18	3.16	17.55	102	235	8	102
14	6.24	2.2	29.17	212	542	13	293
15	3.72	3.14	12	46	83	6	46
16	3.55	3.46	15.17	65	122	8	65
17	7.72	1.76	42.96	369	1018	20	518
18	6.09	2.05	32.99	268	735	15	376
19	4.09	3.46	15.17	65	122	8	65

Table-2: Amino acids and their topological indices, used in present study.

QSPR Models for the Heat Capacity (Cv), Entropy(S) and Thermal Energy (E_{th})

The best linear model for Cv, S and E_{th} contains three topological descriptors, namely, Wiener polarity (Wp), Wiener (W) and Szeged (Sz) indices.

The statistical items of the best three descriptors correlation model were as follows:

Model 1

$$C_v = 60.243 + 7.396(Wp) + 0.829(W) - 0.595(Sz)$$
 (1)

N=19, R=0.963, R^2 =0.928, R^2_{adj} =0.913 RMSE=75.686, F=64.120, Sig=0.000, DW=1.115

Model 2

$$S = 290.743 + 7.773(Wp) + 1.668(W) - 1.102(Sz)$$
 (2)

N=19, R=0.944, R^2 =0.890, R^2_{adj} =0.868 RMSE=117.576, F=40.627, Sig=0.000, DW=1.084

Model 3

$$E_{th} = 150.806 + 34.627(Wp) - 1.957(Sz) + 2.326(W)(3)$$

N=19, R=0.994, R^2 =0.799, R^2_{adj} =0.759, RMSE=257.991, F=19.857, Sig=0.000, DW=2.375

We studied the relationship between topological indices to the thermal energy (E_{th}) , heat capacity (Cv) and entropy (S) of 19 natural amino acids.

In this study, to find the best model for predict the properties mentioned, we will use the following sections.

Multicollinearity

In regression analysis Collinearity occurs when two predictor variables in a multiple regression have a non-zero correlation. Multicollinearity occurs when more than two predictor variables are intercorrelated. Test multicollinearity as a basis the variance inflation factor (VIF) value of multicollinearity test results using SPSS. If the VIF value lies between 1-10, then there is no multicollinearity, and if the VIF<1 or >10, then there is multicollinearity.

In all our final models, the Multicollinearity has existed, because the values of correlations between independent variables are near to one and VIFs value lies are not use of between 1-10.

Verification and Validation

Verification and validation are the primary processes for quantifying and building confidence (or credibility) in numerical models [33].

In this section for verification and validation of the regression models, we will focus on the Durbin-Watson statistic and unstandardized predicted and residual values. One of the assumptions of regression is that the observations are independent. If observations are made over time, it is likely that successive observations are related. If there is no autocorrelation (where subsequent observations are related), the Durbin-Watson statistic should be between 1.5 and 2.5.

In our all models, the value of Durbin-Watson statistic is close to 2(See eqs.1-3) and hence the errors are uncorrelated.

We studied the validation of linearity between the molecular descriptors in the models 1, 2 and 3. We obtained by SPSS the Pearson coefficient correlation and collinearity statistics as follows Tables (3, 4).

Table-3: Correlation between the molecular descriptors (models 1, 2).

Pearson correlations (models 1,2)				Colline: statisti	Corrected model		
Sz		Wp	W	Tolerance	VIF	VIF	
Sz	1	-0.390	-0.816	0.031	31.990	-	
Wp		1	-0.185	0.090	11.077	-	
W			1	0.036	28.097	1	

Table-4: Correlation between the molecular descriptors (model 3).

		on correlat (model 3)	ions	Collinearity	Corrected model		
Sz		Wp	W	Tolerance	VIF	VIF	
Sz	1	-0.390	-0.816	0.031	31.990	-	
Wp		1	-0.185	0.090	11.077	1	
W			1	0.036	28.097	-	

For models 1-3 the Pearson correlation (Sz, W) is near one, and VIF (Sz),(W) and VIF (Wp)>10, therefore there is a linearity between Sz and W. After removed Sz from these models, we corrected models 1 and 2 as follows:

$$Cv = 107.439 + 0.302(W)$$
 (4)

N=19, R=0.857, R^2 =0.735, R_{adj}^2 =0.720

RMSE=116.698, F=47.184, Sig=0.000, DW=1.404 Q^2_{LOO} =0.9176

$$S = 355.383 + 0.549(W) \tag{5}$$

N=19, R=0.803, R²=0.646, R²_{adj}=0.625, DW=1.202 RMSE=173.398, F=30.96, Sig=0.000, Q^2_{LOO} =0.9721

Similarity model 1 and 2 we obtained corrected model 3 as follows:

$$E_{th} = 255.100 + 24.262(Wp)$$
 (6)

N=19, R=0.808, \mathbb{R}^2 =0.653, \mathbb{R}^2_{adj} =0.632 RMSE=403.853, F=31.922, Sig=0.000, DW=2.091 $\mathbb{Q}^2_{1.00}$ =0.9051

In equations (4-6) Q^2_{LOO} is the squared cross-validation coefficients for leave one out, respectively.

We have computed Q^2_{LOO} (Eq.7) by 50% of data, randomly, that are positive and less than one.

$$Q^{2} = 1 - \frac{\sum (Y_{\bar{t}} - \hat{Y}_{\bar{t}|\bar{t}})^{2}}{\sum (Y_{\bar{t}} - \bar{Y})^{2}} \qquad Q^{2} \le 1$$
 (7)

In the equation (7), the notation i|i indicates is predicted by a model estimated when the i-th sample was left out from the training set.

Regular Residuals

The residual is the difference between the observed and predicted values. Comparison between predicted and observed values of Cv, S and E_{th} of respect natural amino acids show in Table 5.

Fig. (1-3) show the linear correlation between the observed and the predicted heat capacity, entropy and thermal energy values obtained using equations (4-6) respectively.

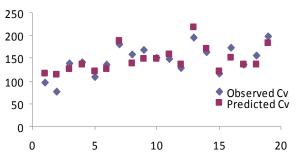


Fig. 1: The predicted versus the observed of heat capacity measured by MLR method.

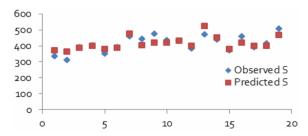


Fig. 2: Comparison between the predicted and observed of entropy by MLR method.

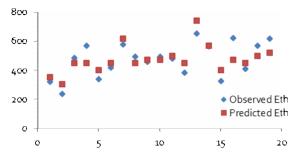


Fig. 3: Scatter plot of the observed versus the predicted thermal energy values by MLR method.

Comp. No.	Observed Cv(J/molK)	Predicted Cv(J/molK)	Residual	Observed S(J/molK)	Predicted S(J/molK)	Residual	Observed E _{th} (kJ/mol)	Predicted E _{th} (kJ/mol)	Residual
1	97.66	116.21	-18.55	335.929	368.412	-32.483	320.347	352.170	-31.823
2	76.36	112.88	-36.52	309.169	363.470	-54.301	237.779	303.635	-65.856
3	137.64	127.09	10.55	389.576	384.587	4.989	486.677	449.240	37.437
4	141.45	136.47	4.98	403.027	398.514	4.513	567.268	449.240	118.028
5	108.28	121.35	-13.07	351.032	376.050	-25.018	338.889	400.705	-61.816
6	135.52	127.09	8.43	388.372	384.587	3.785	418.309	449.240	-30.931
7	181.91	188.48	-6.57	458.989	475.792	-16.803	578.499	619.113	-40.614
8	157.78	138.28	19.50	441.638	401.210	40.428	495.184	449.240	45.944
9	168.88	148.56	20.32	473.731	416.486	57.245	457.129	473.508	-16.379
10	151.18	148.56	2.62	433.294	416.486	16.808	494.042	473.508	20.534
11	148.54	157.33	-8.79	429.624	429.515	0.109	480.917	497.775	-16.858
12	127.92	136.47	-8.55	383.088	398.514	-15.426	382.800	449.240	-66.440
13	195.91	219.02	-23.11	469.355	521.170	-51.815	653.915	740.450	-86.535
14	163.76	171.54	-7.78	439.163	450.632	-11.469	564.124	570.578	-6.454
15	117.33	121.35	-4.02	370.331	376.050	-5.719	323.607	400.705	-77.098
16	173.87	150.68	23.19	456.556	419.631	36.925	623.819	473.508	150.311
17	136.38	136.47	-0.09	389.901	398.514	-8.613	408.779	449.240	-40.461
18	155.85	135.26	20.59	415.053	396.717	18.336	570.842	497.775	73.067
19	198.99	182.13	16.87	504.868	466.357	38.511	617.992	522.043	95.949

Table-5: Comparison between predicted and observed values of the heat capacity (Cv), entropy (S) and thermal energy (E_{th}) of respect AAs.

Conclusion

In this study, QSPR mathematical models for the prediction of the heat capacity (Cv), entropy (S) and thermal energy(E_{th}) of amino acids by using MLR method based on topological descriptors calculated from molecular structure alone have been developed.

MLR model is proved to be a useful tool in the prediction of Cv, S and E_{th} . Cross-validation as the evaluation technique has been designed to evaluate the quality and predictive ability of the MLR model. The obtained results showed that the only one topological index (W) for predicting Cv and S. Wiener polarity index is good topological index for modeling thermal energy.

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